

# Mapping the subglacial hydrology network with **a** dense seismic array

## A multi-method approach.

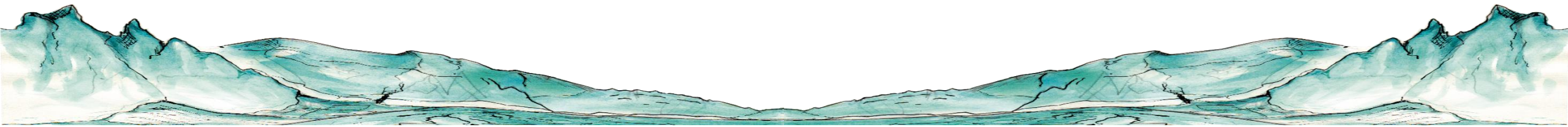
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AMERICAN GEOSCIENCES UNION, SAN FRANCISCO 2019

**Ugo NANNI**<sup>1</sup>, Florent GIMBERT<sup>1</sup>, Philippe ROUX<sup>2</sup>, Albane LECOINTRE<sup>2</sup>

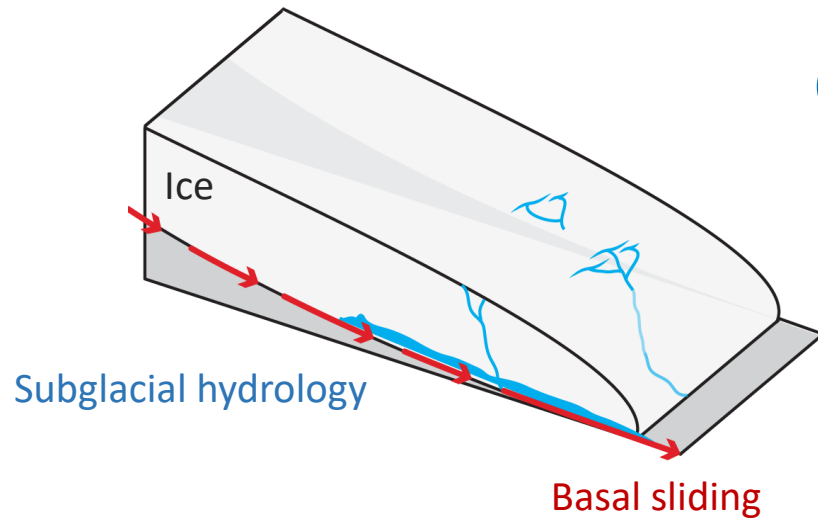
<sup>1</sup> UNIV GRENOBLE ALPES, CNRS, IRD, IGE, GRENOBLE, FRANCE

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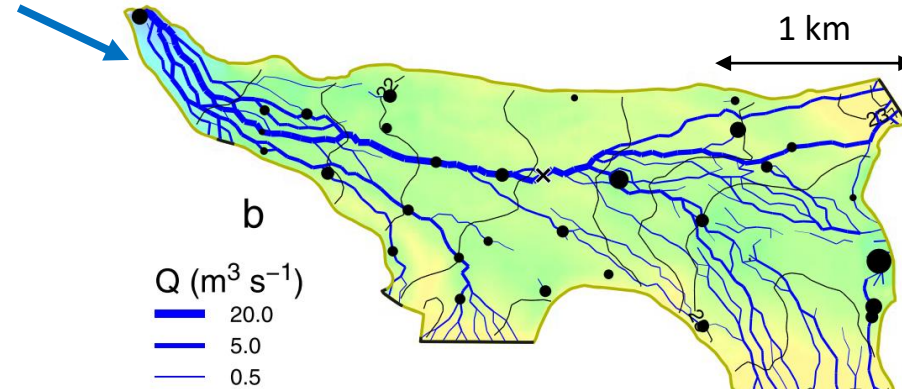
# About subglacial hydrology

- Subglacial water conditions :
  - Control **sliding** by **lubrication**



- Complex drainage system:
  - **Channels** : spatially discrete
  - **Cavities** : spatially distributed

## Channels

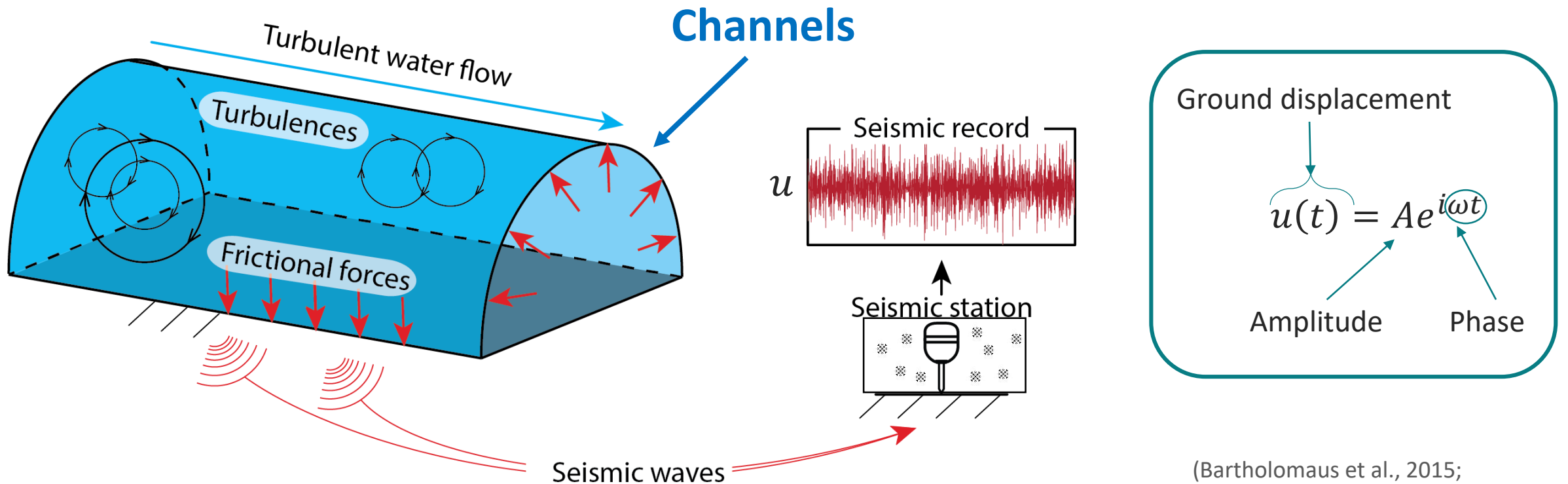


Subglacial drainage system as modelled by Werder et al., 2013

→ Complex physical process but **limited observations**

# Subglacial channel flow induced noise

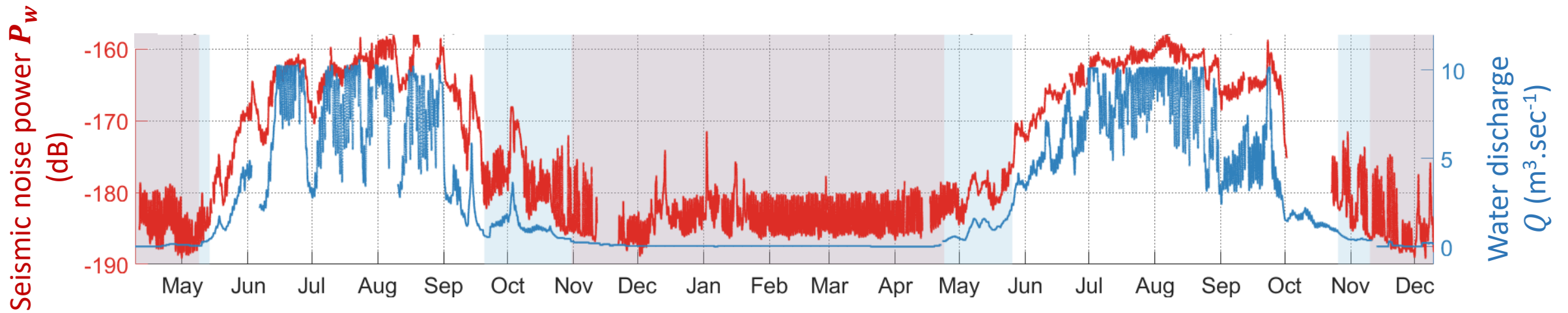
- Subglacial turbulent water flow generates continuous seismic noise ( $\sim [2-20]$  Hz)



(Bartholomäus et al., 2015;  
Gimbert et al., 2016;)

# Seismic power in the [3 – 10] $Hz$ band

- Good sensitivity to subglacial water discharge:
  - Continuous signal over melt season



(Nanni et al., 2019)

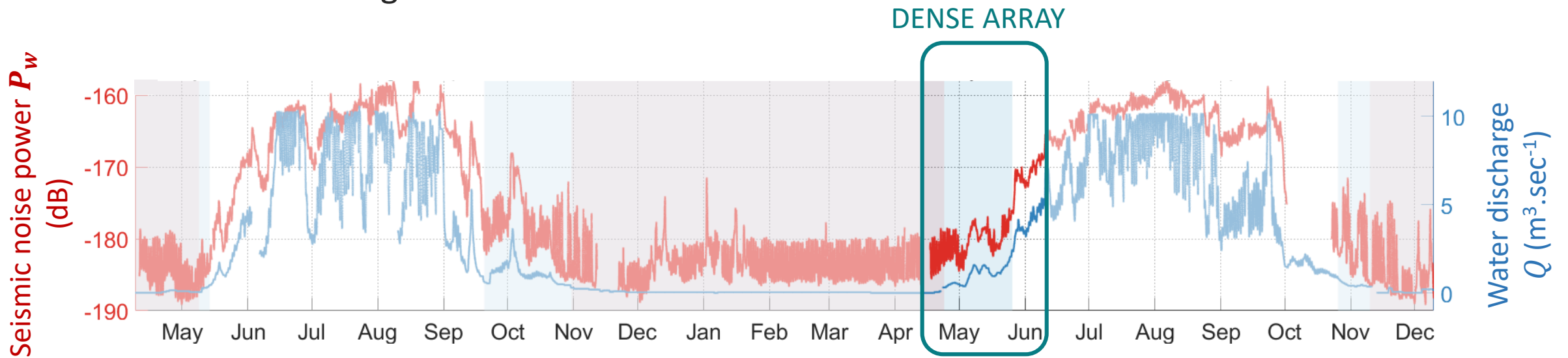
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→ Lacking **spatial** and **phase** information



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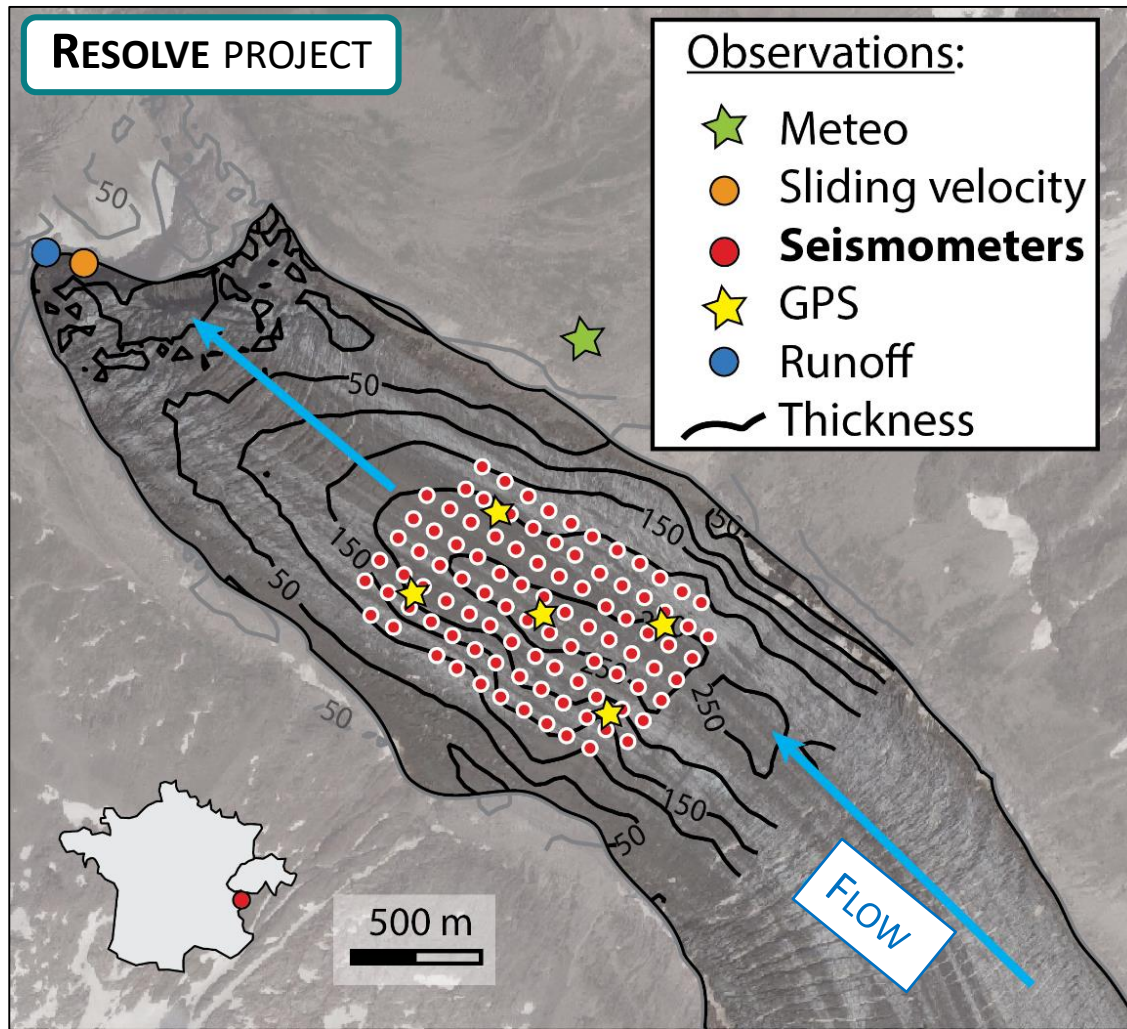


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# Challenge: locate continuous noise source(s)

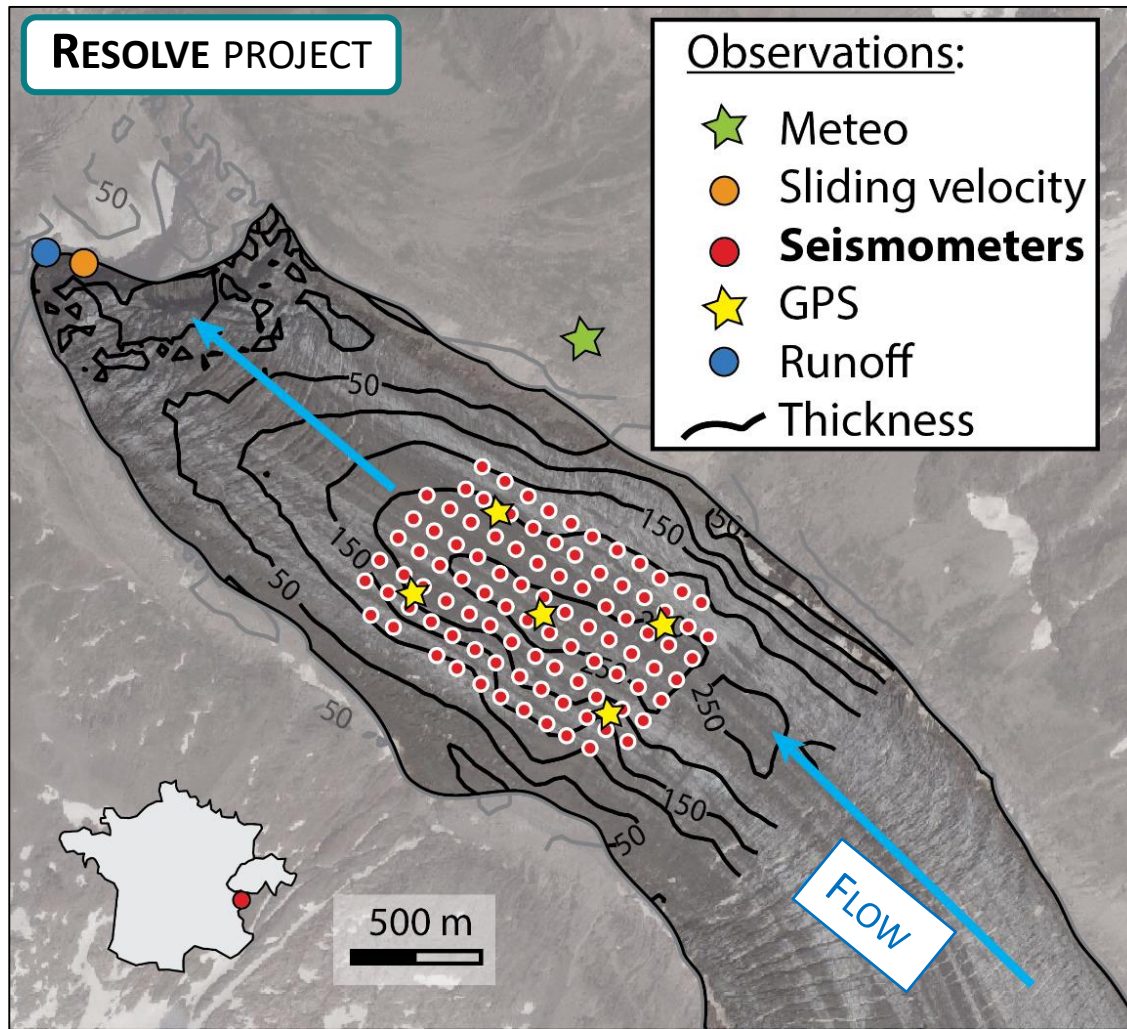


- 1 month when channels develop
- 100 seismometers





# Challenge: locate continuous noise source(s)



- Typical frequencies :  $[3 - 20] Hz$
- Typical wavelengths :  $\lambda \sim [500 - 75] m$
- Inter-stations distance:  $40 m$
- Glacier thickness:  $\sim 250 m$

- Sub-wavelength array
- Near-field propagation

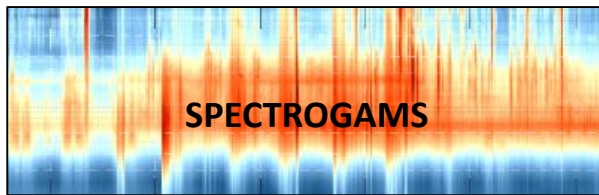
**UNIQUE SETUP !**

# Methods: locate continuous noise source(s)

1

## Amplitude analysis

~ energy differences



- Seismic power  $P_w$  spatial variability:
  - Source surface signature
  - **Dominant** sources in time

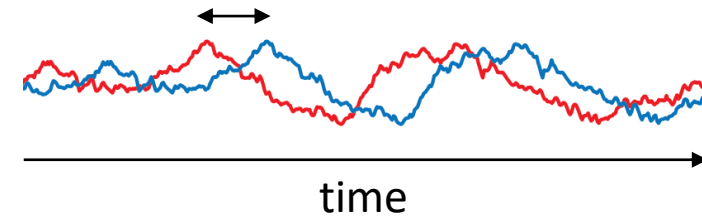
$$u(t) = Ae^{i\omega t}$$

Amplitude      Phase

## Phase analysis

2

~ time delays



- **Phase difference averaging (> 1 h) prior to locating:**
  - Stack phase differences: keep **coherent** signal

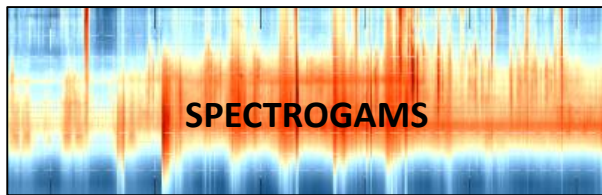


# Methods: locate continuous noise source(s)

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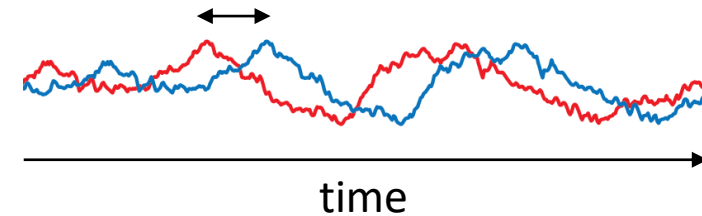
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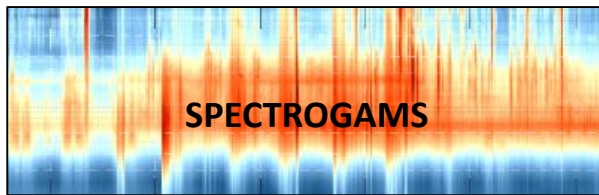
- Use long-term period (> 1 h). NOT SUITABLE
  - Stack phase differences: keep coherent signal

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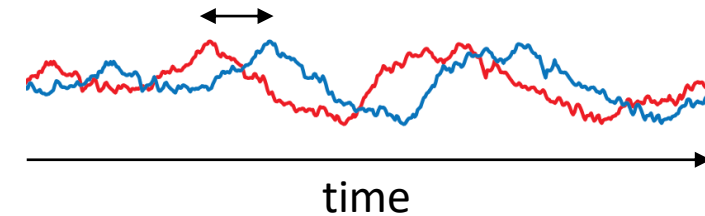
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Amplitude      Phase

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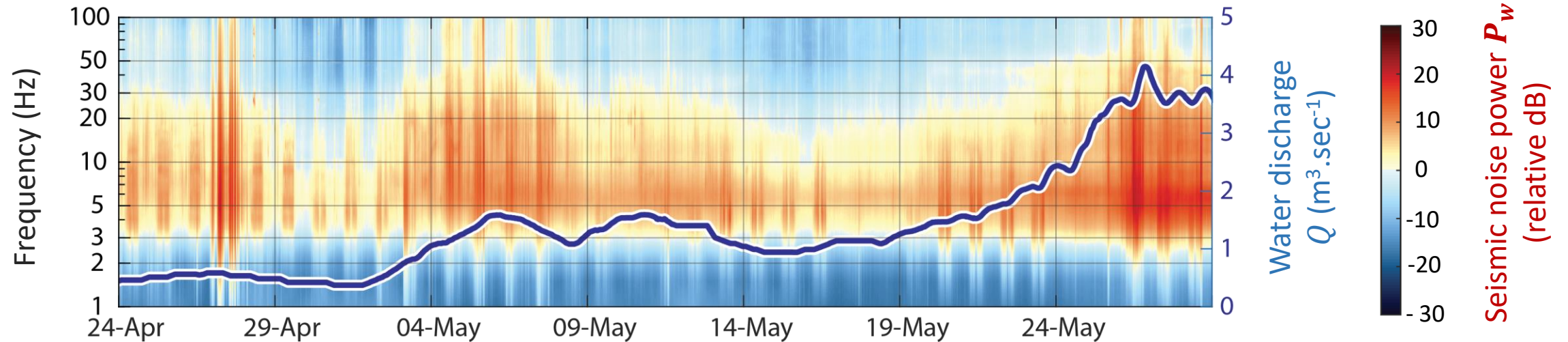


- Use long-term period ( $> 1$  h). NOT SUITABLE
  - Stack phase differences: keep coherent signal
- Perform location analysis at short timescales (1 sec), and then look at location density maps :  
(e.g. Corciulo et al., 2012)
  - Phase coherence = individual source location

$$u(t) = Ae^{i\omega t}$$

# Median amplitude evolution

- High  $P_w$  in the [3 – 20] Hz frequency range concomitant with increasing  $Q$



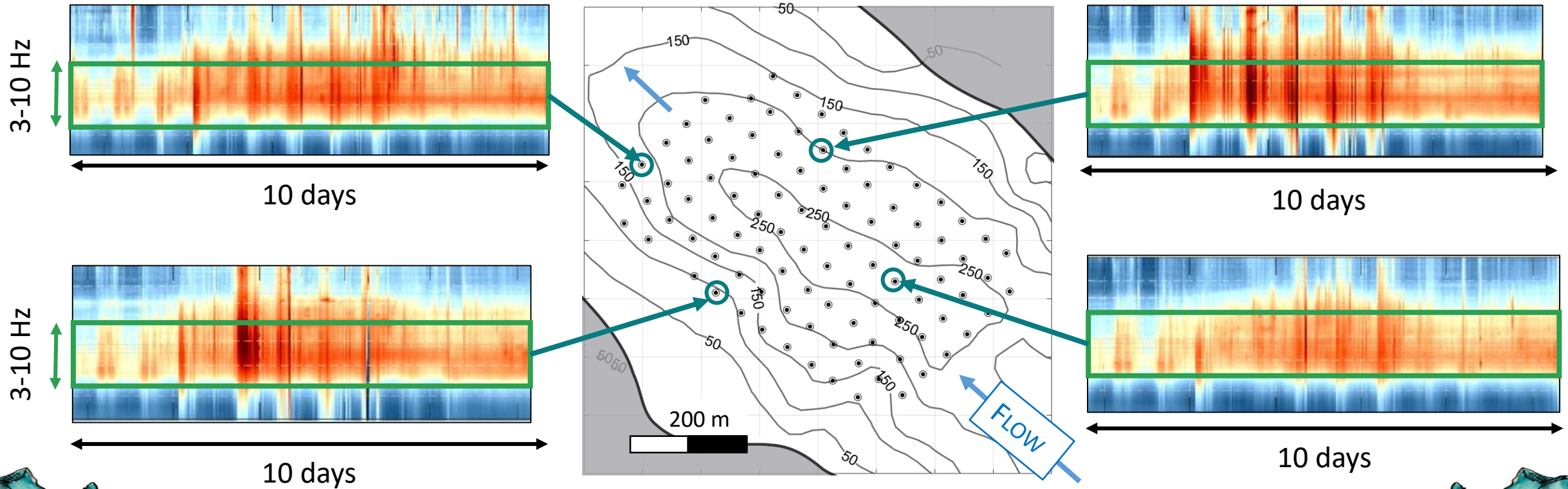
→ Amplitude dominated by turbulent water flow induced noise



$$u(t) = Ae^{i\omega t}$$

# Amplitude analysis

- Compute  $P_w$  spatial anomaly **over 2 hours**



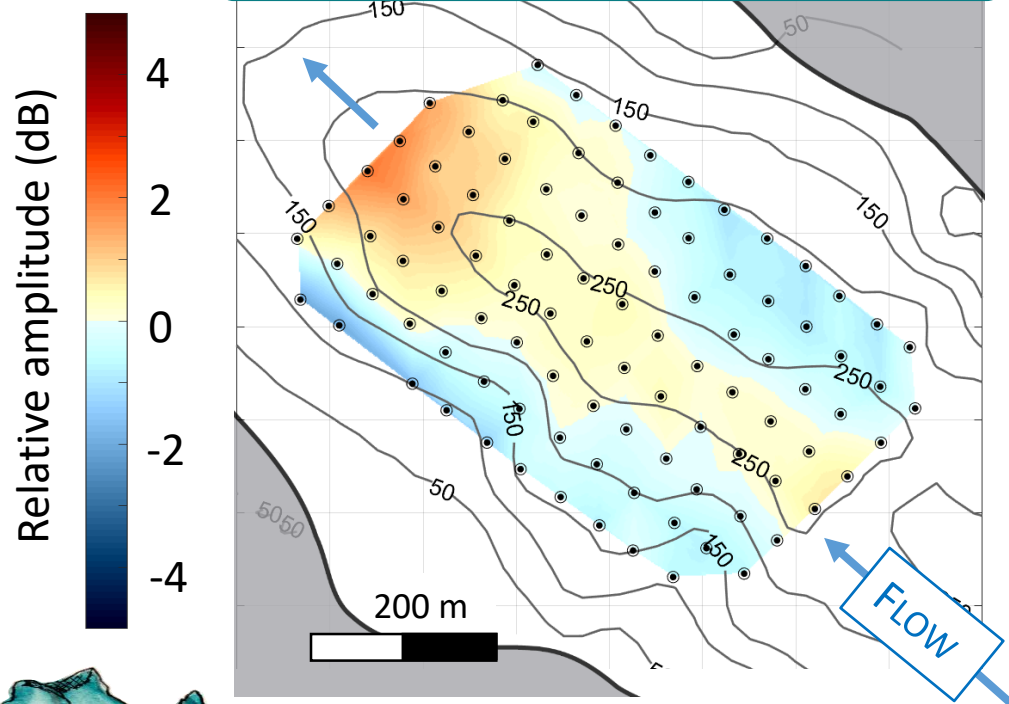


$$u(t) = A e^{i\omega t}$$

# Amplitude spatial variations

- Compute 2 hour- $P_w$  spatial anomaly: stack **over the whole period**

Median anomaly over 30 days

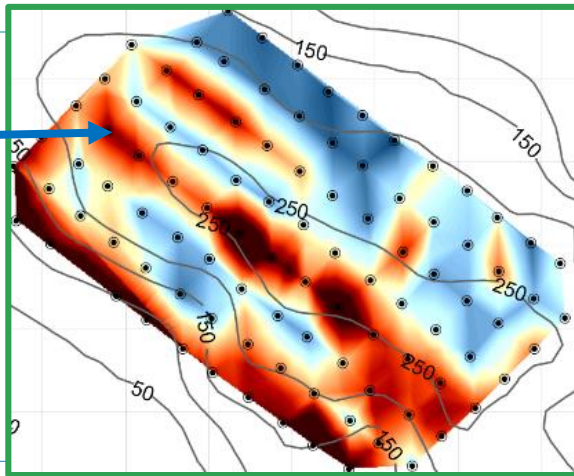


- Higher *power* downstream
- Higher *power* in the middle
- $\sim 100$  m variations

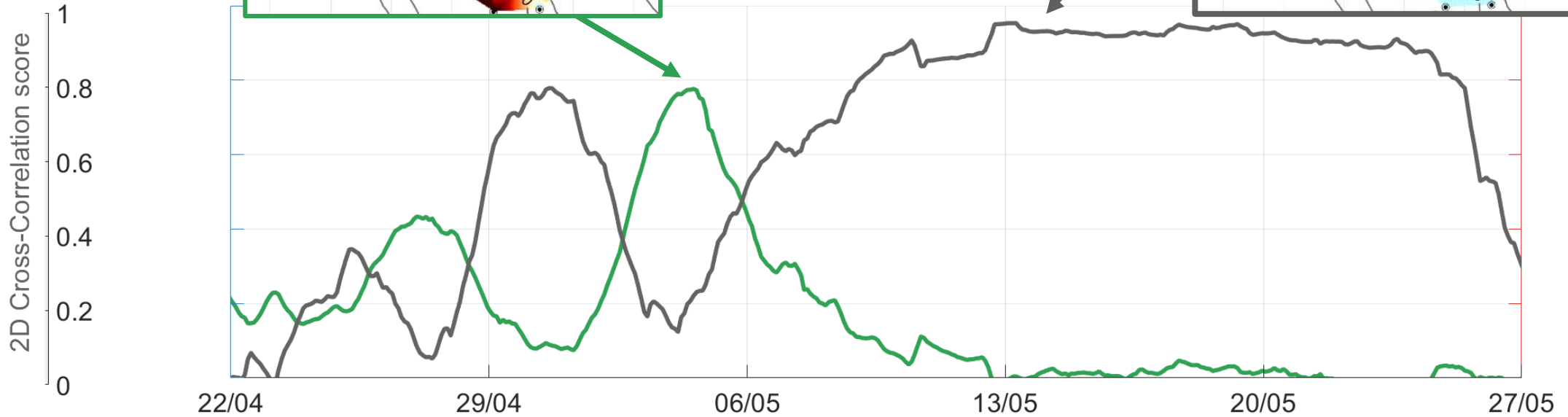
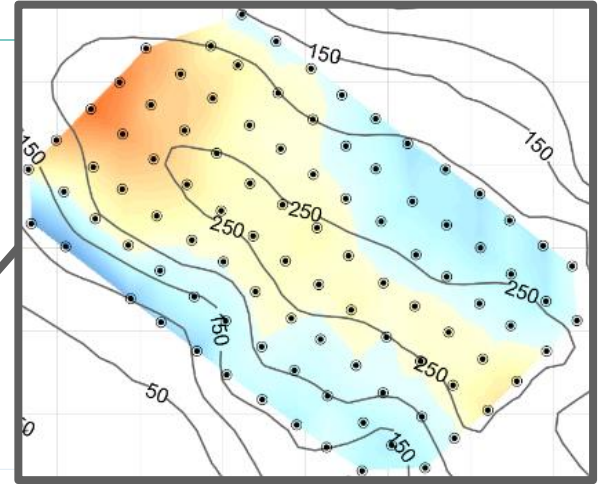


$u(t) = Ae^{i\omega t}$  Amplitude spatio-temporal variations

Channels ?



Temporal occurrences of key patterns

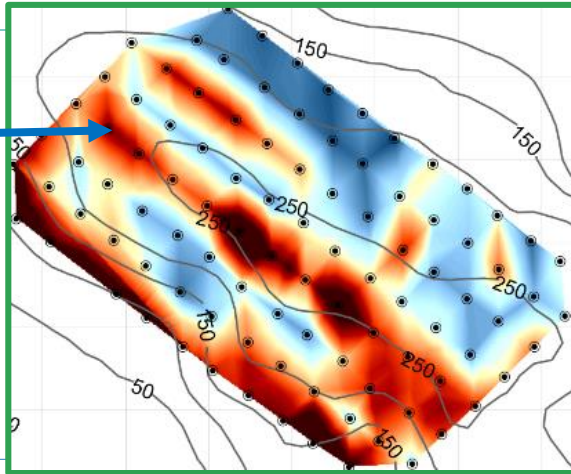




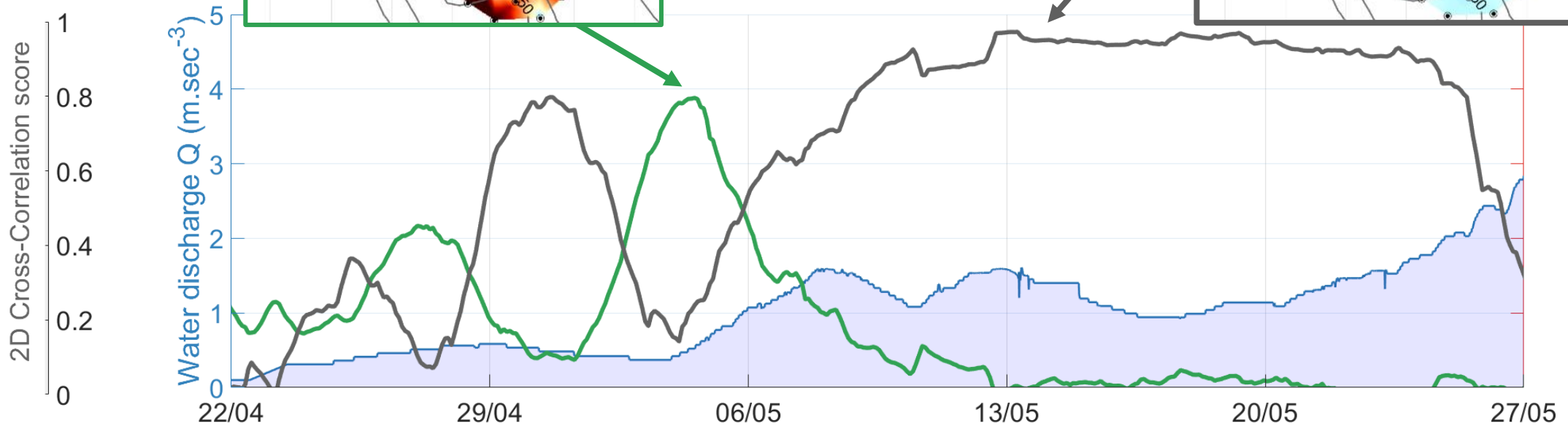
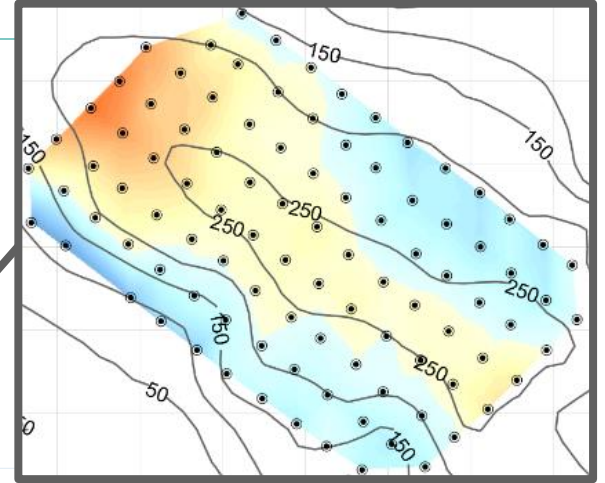
$$u(t) = Ae^{i\omega t}$$

# #1 CAPABLE TO CAPTURE CHANNELS DEVELOPMENT

Channels ?



Channel pattern appears concomitantly to  $Q$  rise



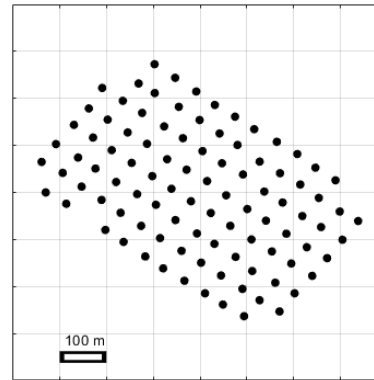


$$u(t) = Ae^{i\omega t}$$

# The beam former method

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Source location

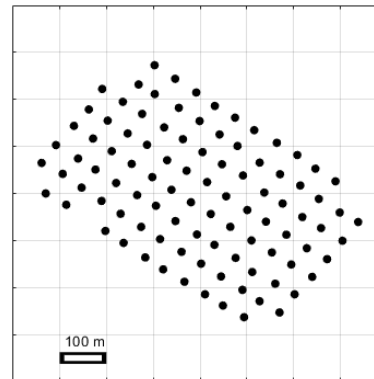


$$u(t) = Ae^{i\omega t}$$

# The beam former method

- Assume a unique source over 1 second-signal
- Minimize misfit  $|\text{Phase}_{\text{model}} - \text{Phase}_{\text{observed}}|$  (*gradient-based minimization*)

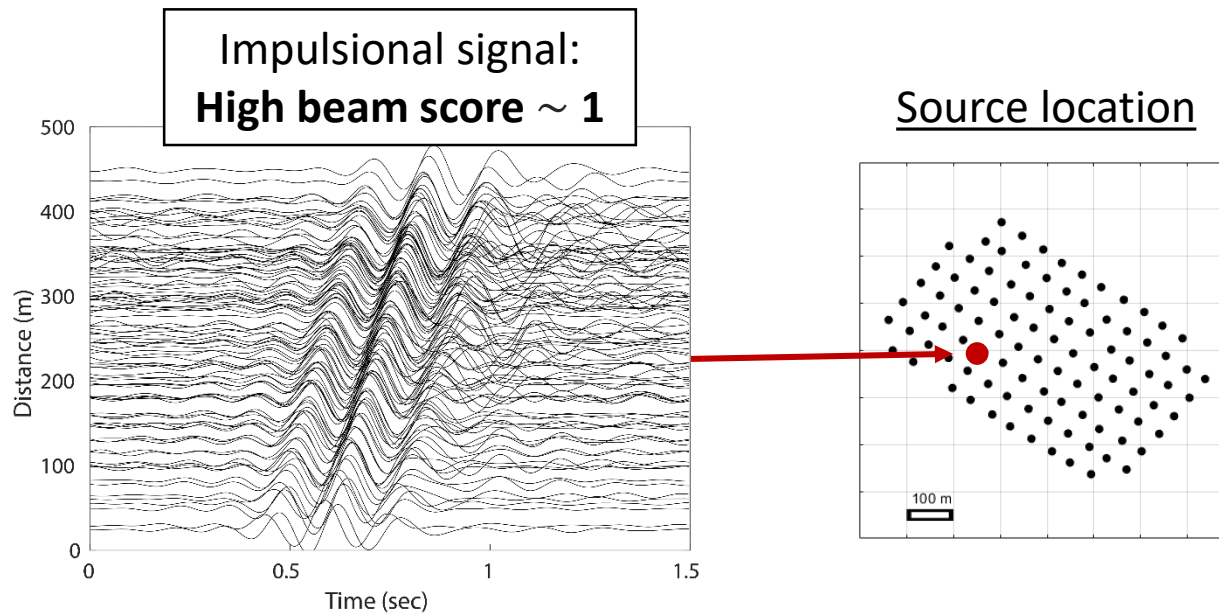
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# The beam former method

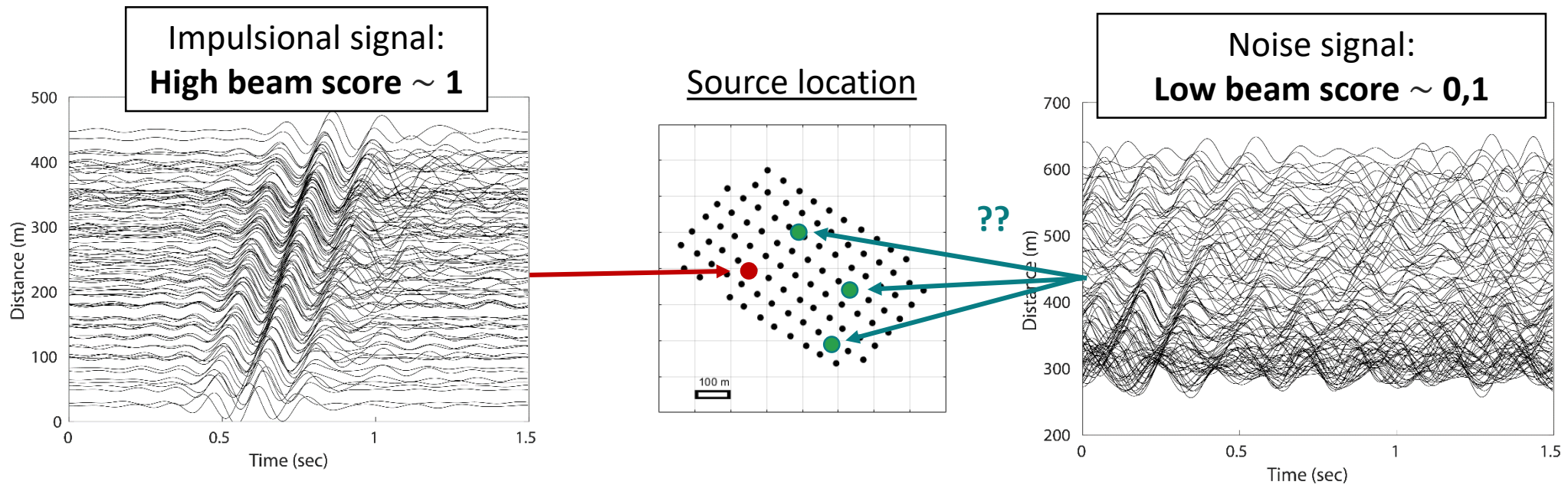
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- Beam score  $\propto$  phase coherency  $\sim$  location accuracy



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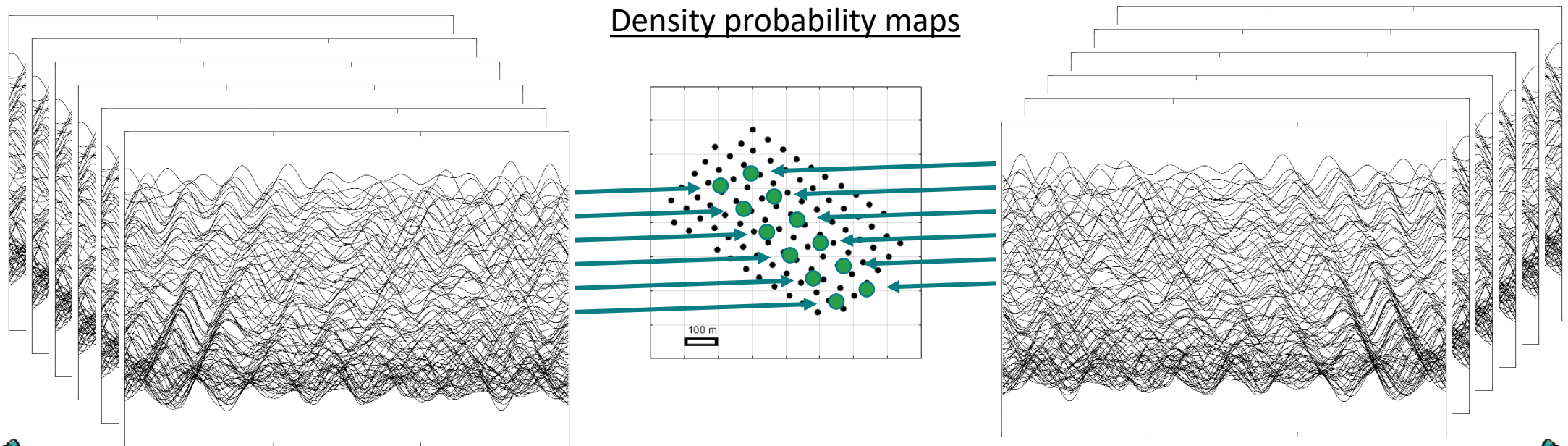




$$u(t) = Ae^{i\omega t}$$

# Increasing location precision

- Subglacial water flow: **low beam** score (**several sources are active simultaneously**)
- We stack 1 second-location over long time periods ( $\sim$  days)

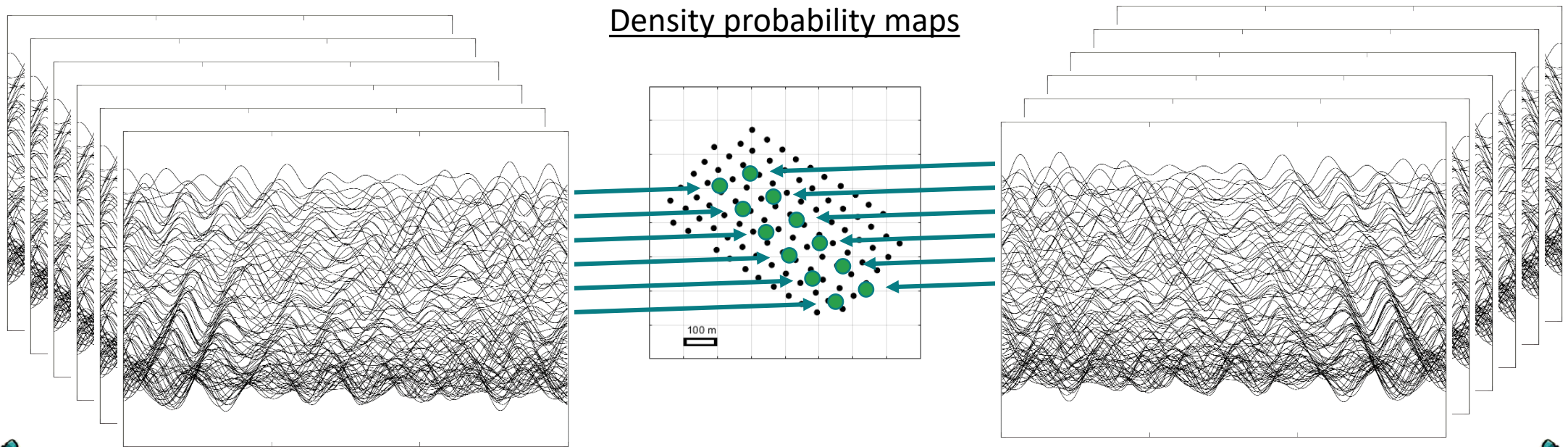


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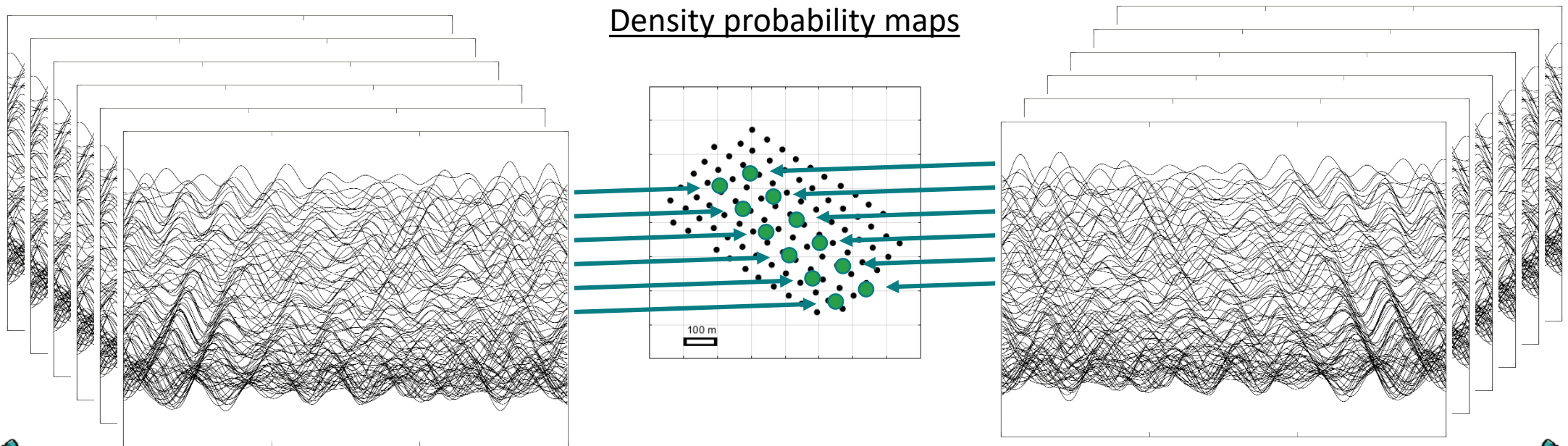




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# Increasing location precision

- Subglacial water flow: **low beam** score (noise)
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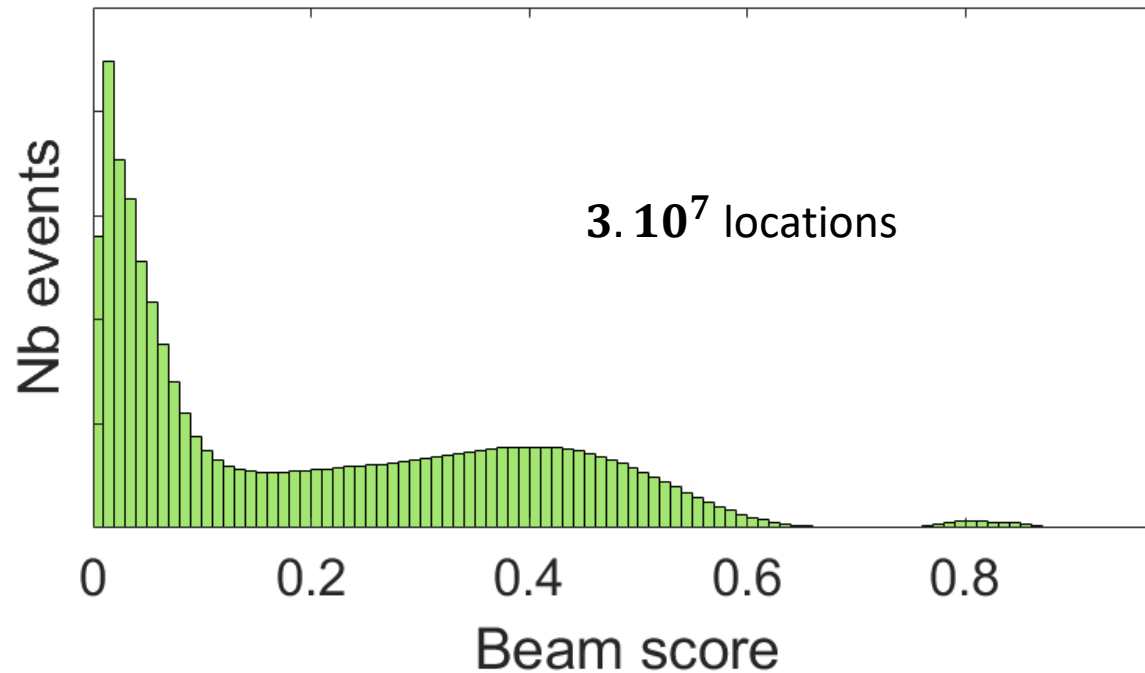




$$u(t) = Ae^{i\omega t}$$

# Beam score ranges over 10 days (5 Hz)

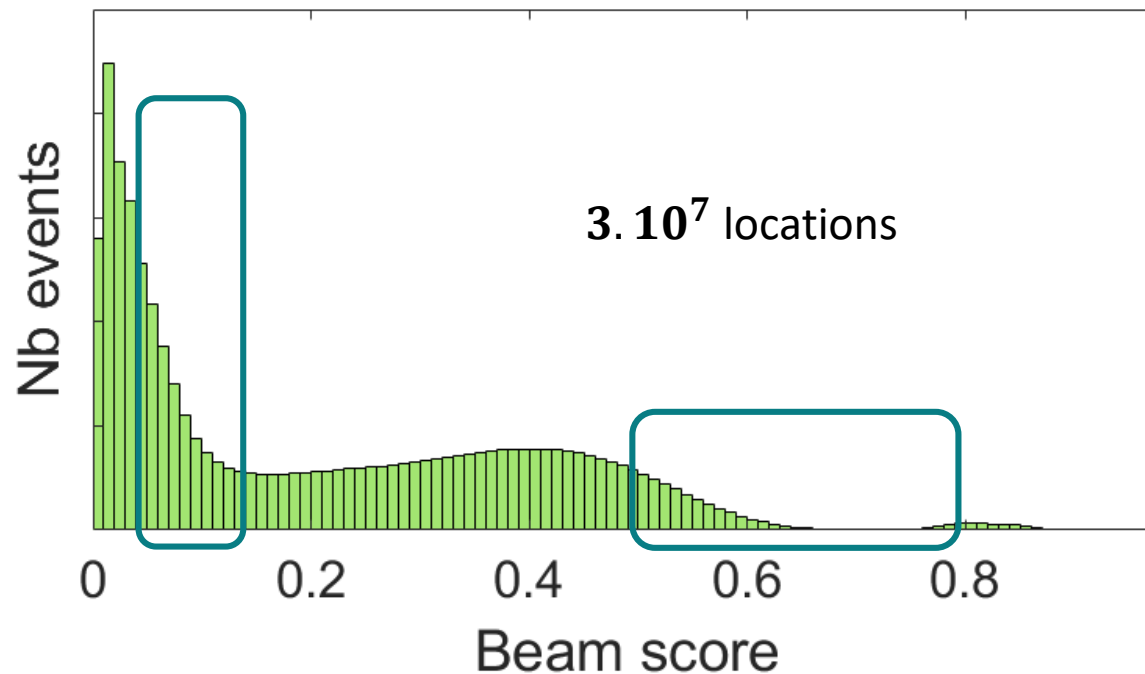
- Most location are associated with low beam scores ( $< 0,2$ )



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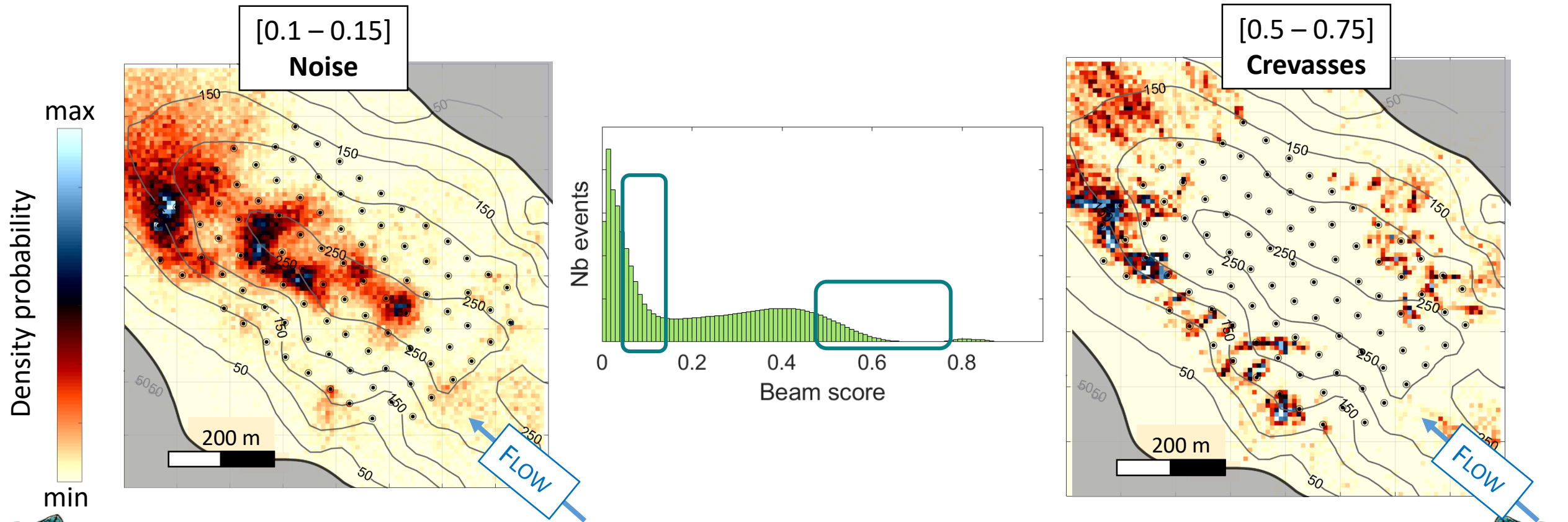
- Most location are associated with low beam scores ( $< 0,2$ )
  - Select 2 beam score ranges
  - Select coherent phase velocities [ $1400 - 2400 \text{ m. sec}^{-1}$ ] and depth



$$u(t) = Ae^{i\omega t}$$

# Beam score ranges over 10 days (5 Hz)

- Distinct features with coherent phase velocities [1400 – 2400  $m \cdot sec^{-1}$ ] and depths

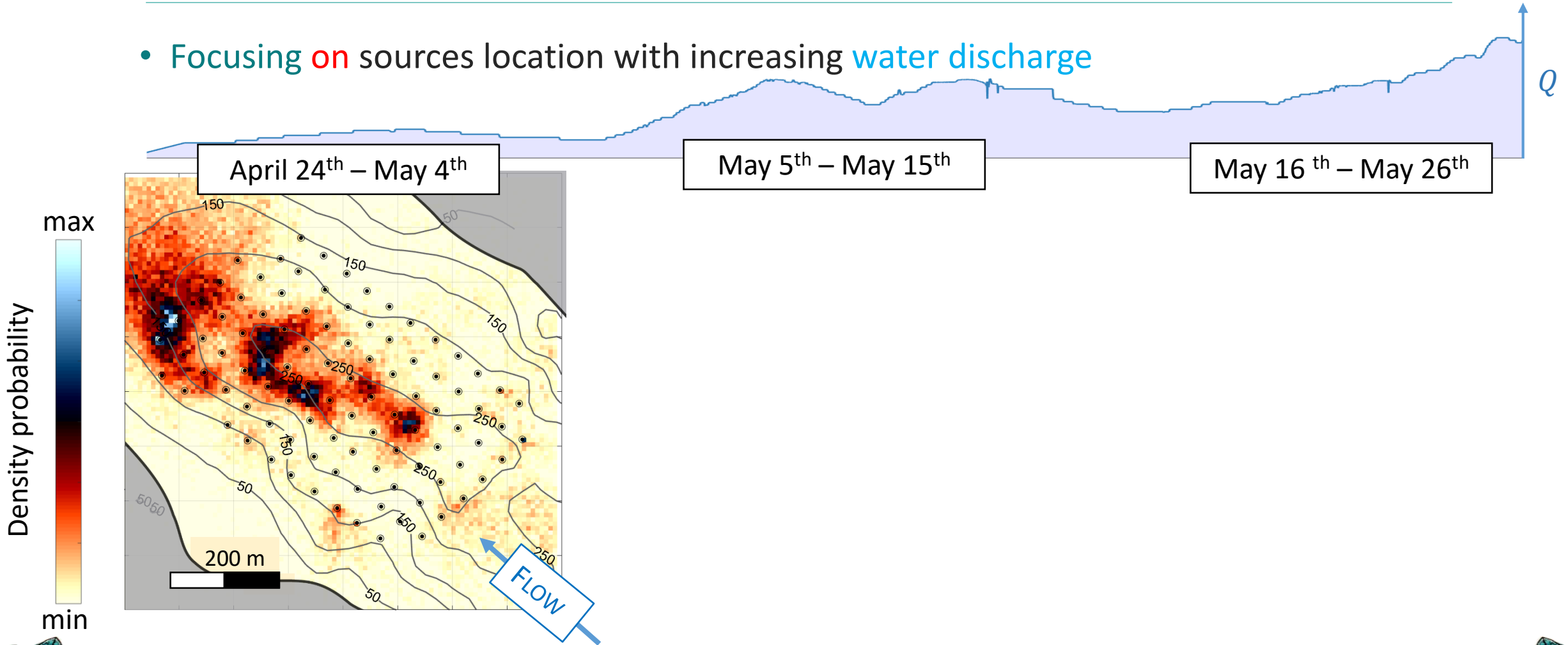




$$u(t) = Ae^{i\omega t}$$

# Spatial patterns at low beam score

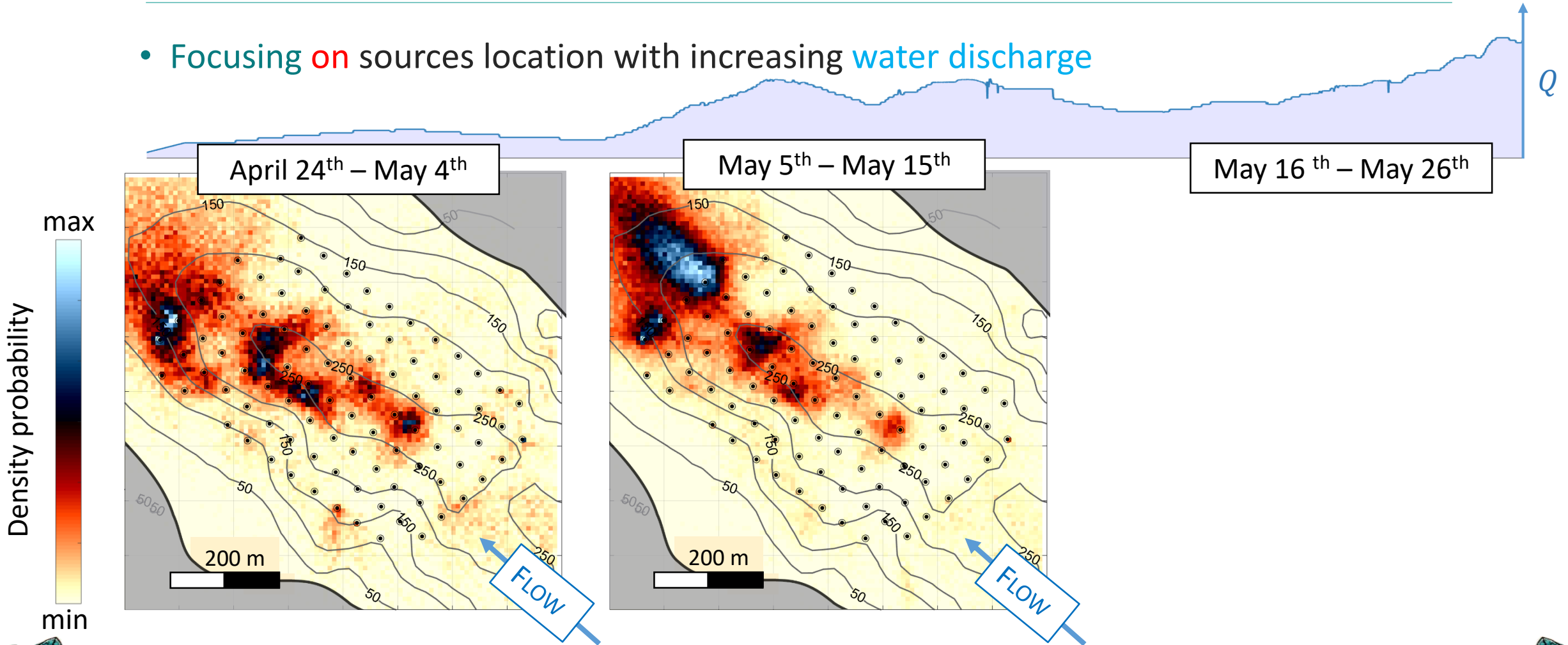
- Focusing on sources location with increasing water discharge



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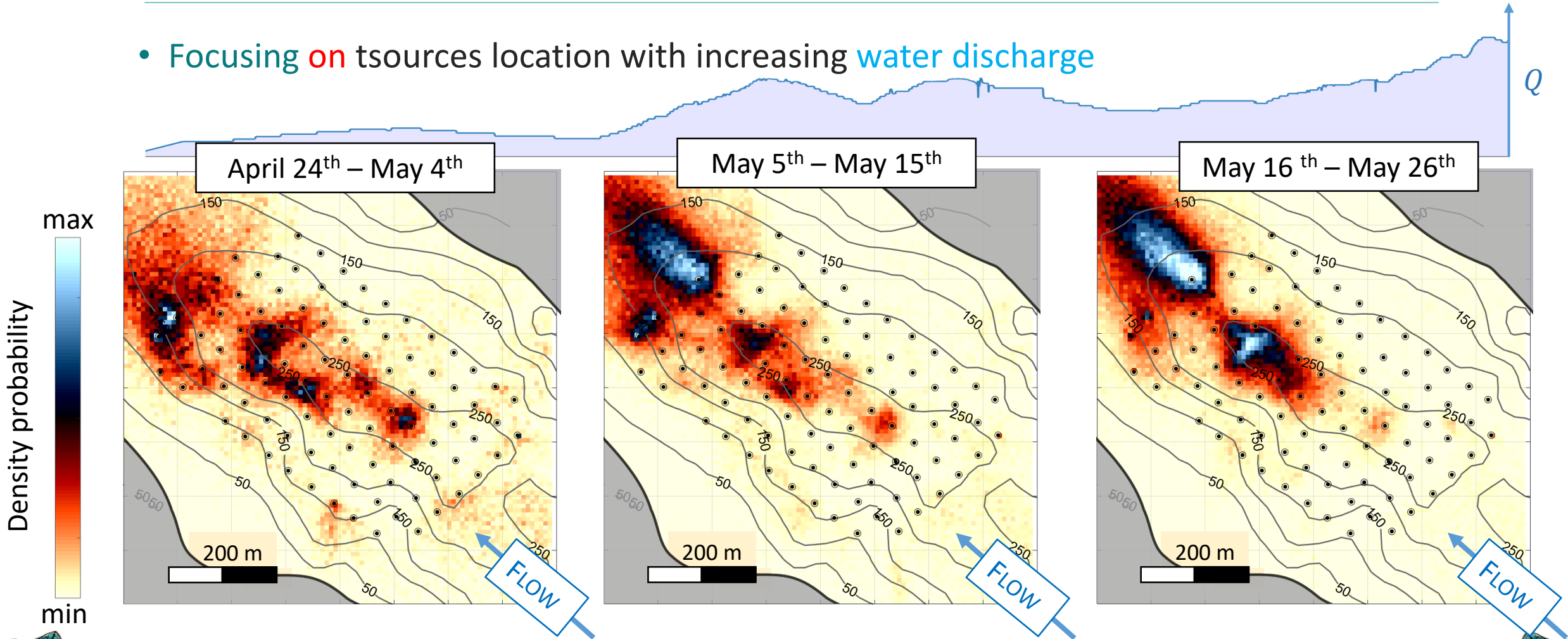
- Focusing **on** sources location with increasing **water discharge**



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# Spatial patterns at low beam score

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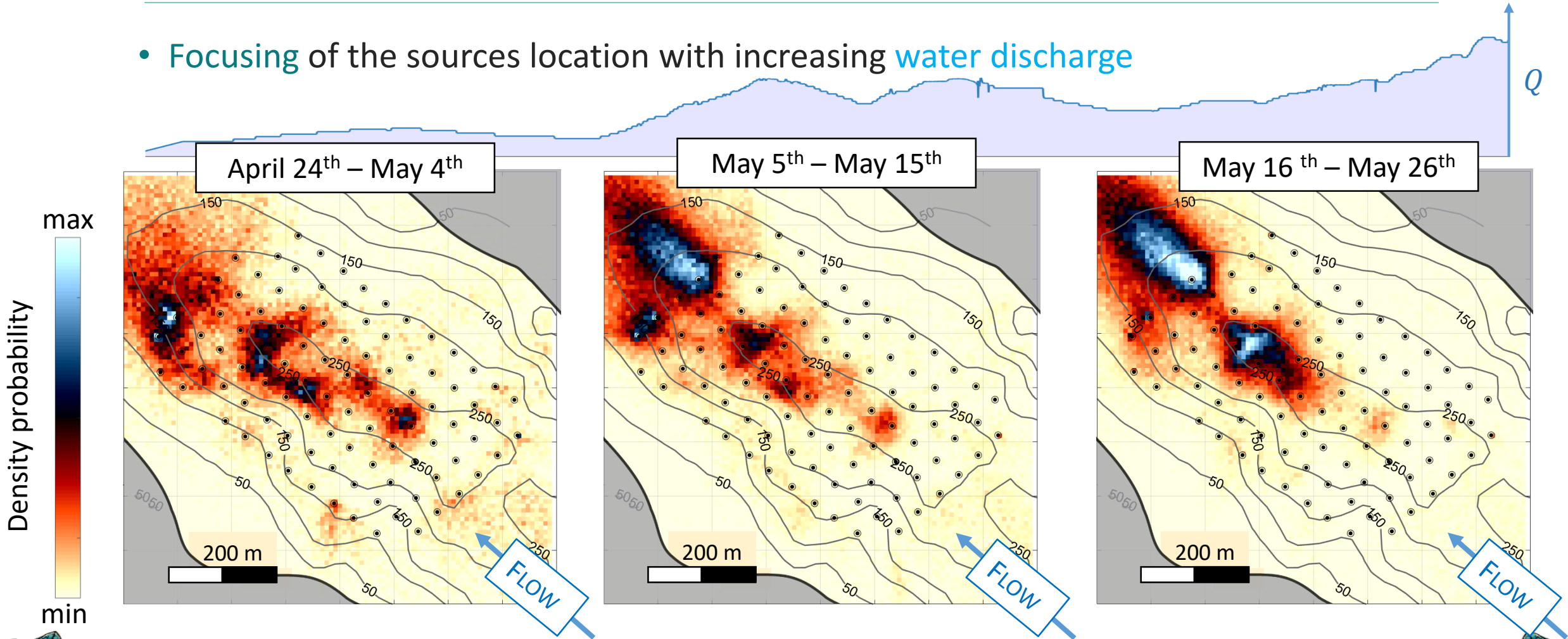
(Nanni et al., in prep.)



$$u(t) = Ae^{i\omega t}$$

## #2 CAPABLE TO CAPTURE CHANNELS EVOLUTION

- Focusing of the sources location with increasing water discharge



(Nanni et al., in prep.)

# Conclusions

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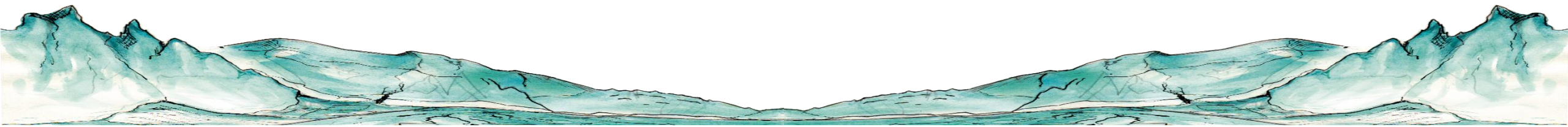
## Amplitude spatial anomaly

- ✓ Capture noise sources changes
- ✓ Capture **channelization onset**

## Complementary

## Phase analysis (1 sec-beamformer)

- ✓ **Allows retrieving** multiple noise source
- ✓ **Captures** channels location **continuously**
- ✓ Capture **subglacial hydrology evolution**
- ✓ **Allows for localization** < 20 m resolution



# Conclusions & Perspectives

## Amplitude spatial anomaly

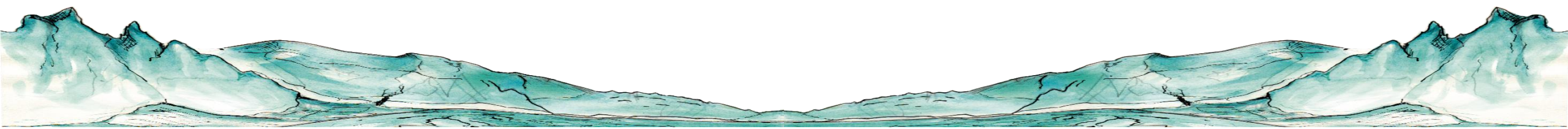
- ✓ Capture noise sources changes
- ✓ Capture **channelization onset**
- ~ Channels not observed full-time
- ~ Influence of near field-propagation
- ~ Spatial heterogeneity of  $\lambda/6$

## Complementary

## Phase analysis (1 sec-beamformer)

- ✓ Sensitive to multiple noise source
- ✓ Statistically capture channels location
- ✓ Capture **subglacial hydrology evolution**
- ✓  $< 20 m$  resolution
- ~ Requires multi-day stacking

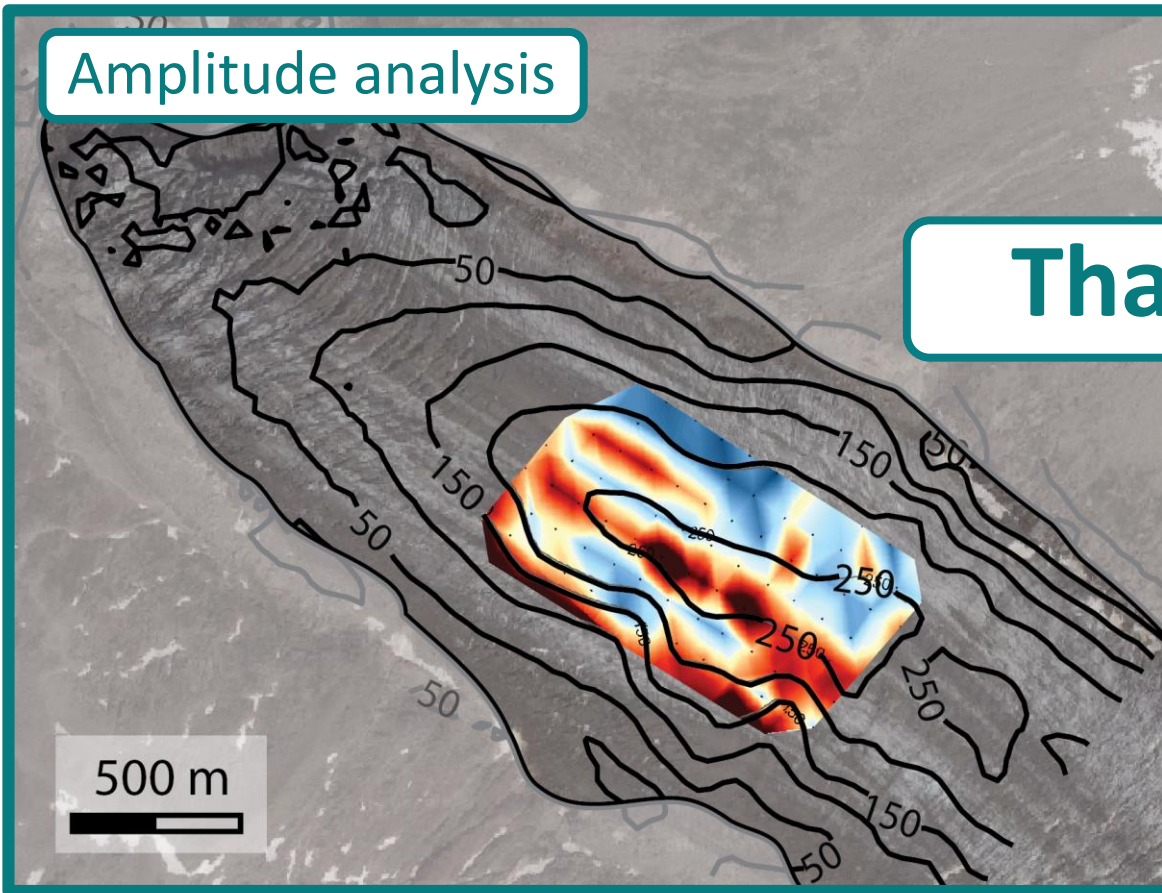
▶ Needs for full-waveform modelling (?)



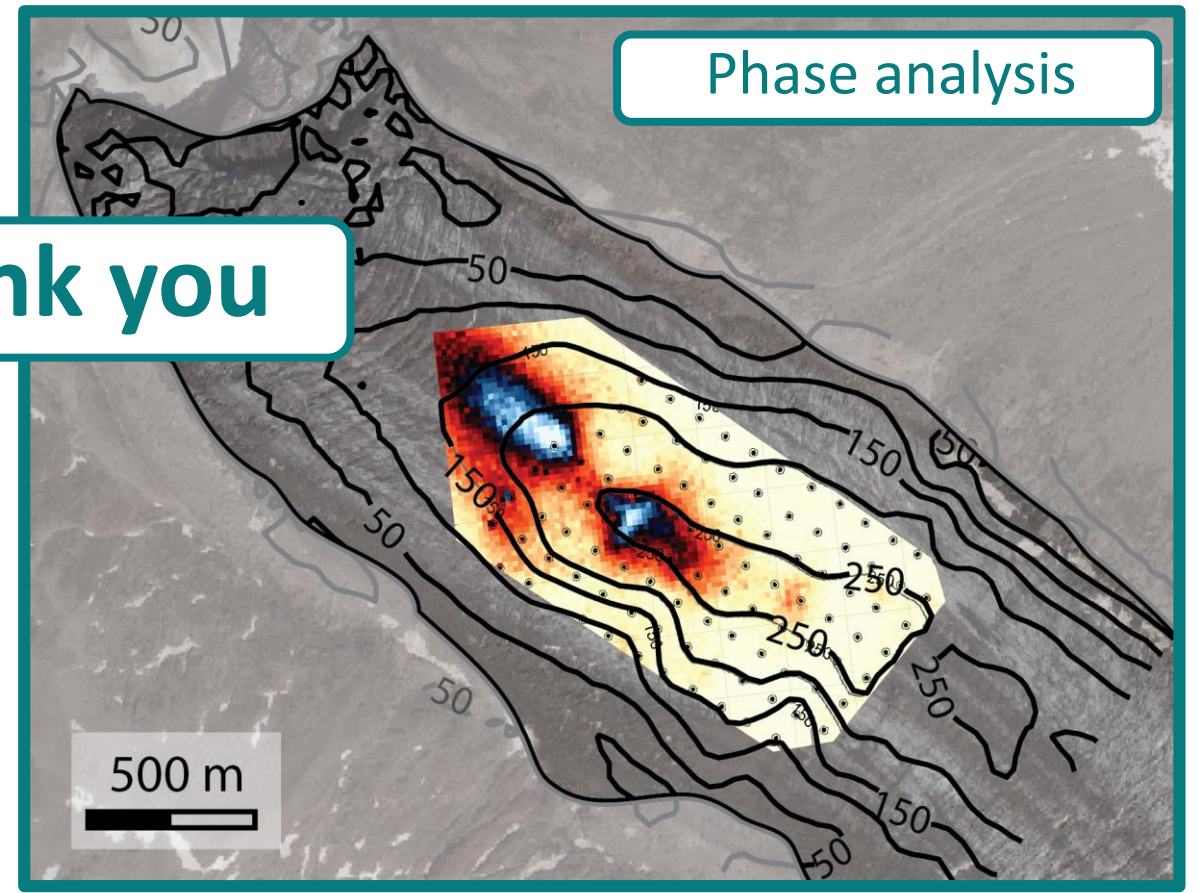


We can map **the** subglacial hydrology **network** with dense array seismology

Amplitude analysis



Phase analysis



Thank you

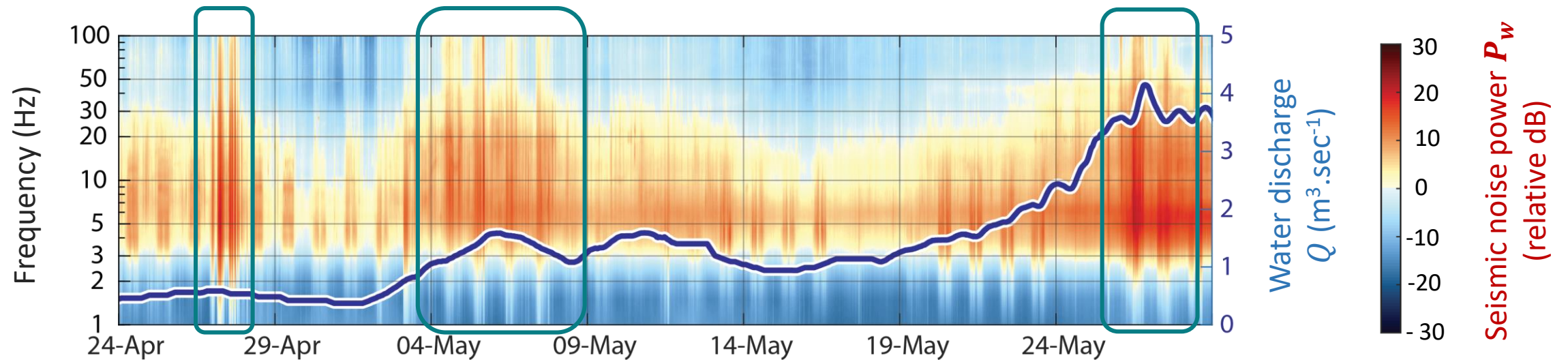
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# Median amplitude evolution

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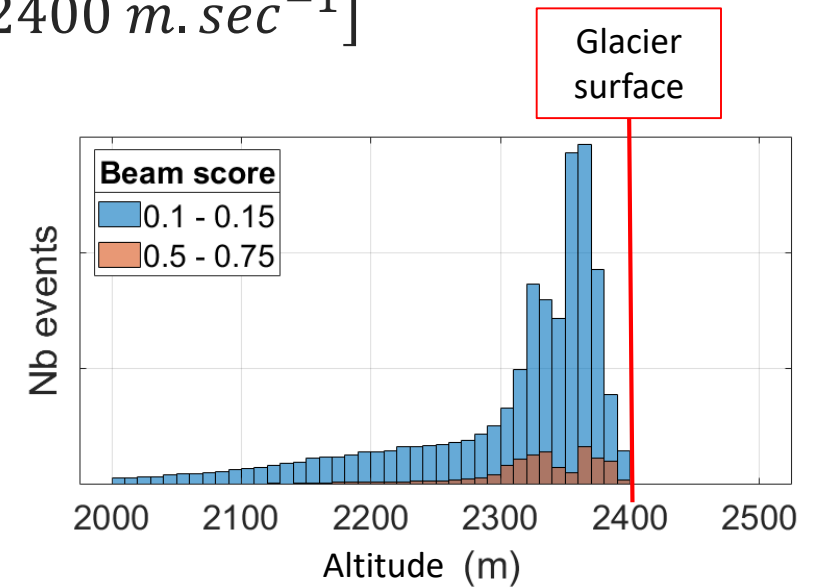
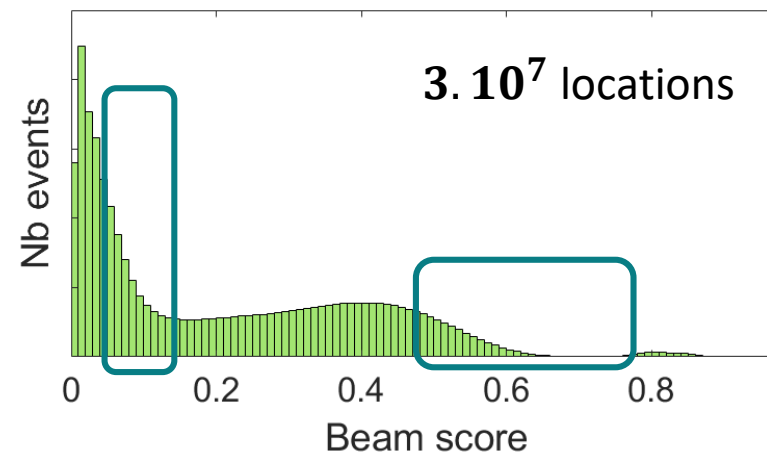
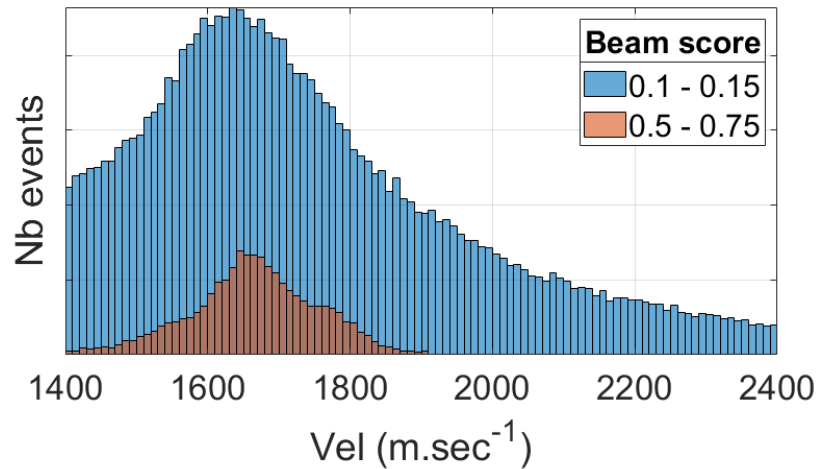


→ Amplitude dominated by turbulent water flow induced noise

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# Beam score ranges over 10 days (5 Hz)

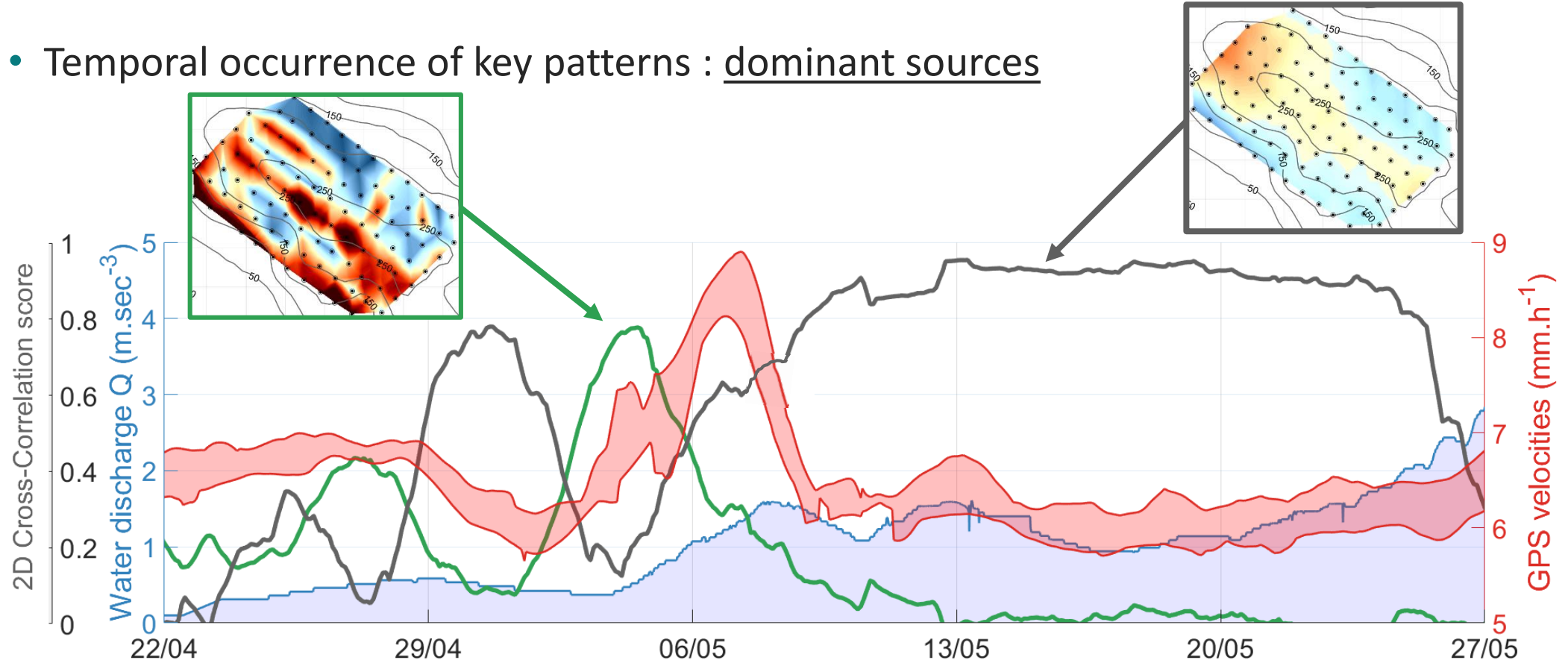
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  - Select coherent phase velocities and depth [1400 – 2400  $m.sec^{-1}$ ]





$u(t) = Ae^{i\omega t}$  Amplitude spatio-temporal variations

- Temporal occurrence of key patterns : dominant sources



(Nanni et al., in prep.)

- Concomitant to  $Q$  rise
- Concomitant to glacier acceleration